A tourist guide to the RCSR

Some of the sights, curiosities, and little-visited by-ways

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RCSR is a **Reticular Chemistry Structure Resource** available at http://rcsr.net. It is open every day of the year, 24 hours a day, and admission is free. It consists of data for polyhedra and 2-periodic and 3-periodic structures (nets). Visitors unfamiliar with the resource are urged to read the "about" link first. This guide assumes you have.

The guide is designed to draw attention to some of the attractions therein. If they sound particularly attractive please visit them. It can be a nice way to spend a rainy Sunday afternoon.

OKH refers to M. O'Keeffe & B. G. Hyde. *Crystal Structures I: Patterns and Symmetry*. Mineral. Soc. Am. 1966. This is out of print but due as a Dover reprint 2019.

POLYHEDRA

Read the "about" for hints on how to use the polyhedron data to make accurate drawings of polyhedra using crystal drawing programs such as CrystalMaker (see "links" for that program). Note that they are Cartesian coordinates for (roughly) equal edge. To make the drawing with unit edge set the unit cell edges to all 10 and divide the coordinates given by 10. There seems to be no generally-agreed best embedding for complex polyhedra. It is generally not possible to have equal edge, vertices on a sphere and planar faces. Keywords used in the search include:

Simple. Each vertex is trivalent (three edges meet at each vertex) **Simplicial.** Each face is a triangle. The dual of a simplicial polyhedron is a simple polyhedron and *vice versa*.

Regular polyhedra. The five regular polyhedra should be well known. they are the: tetrahedron 3⁴ **tet**, octahedron 3⁴ **oct**, icosahedron 3⁵ **ico** cube 4³ **cub**, dodecahedron 5³ **dod**. These are the only polyhedra with one kind of vertex, one kind of edge and one kind of face, i.e. *transitivity* 1 1 1

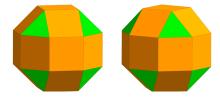
Quasiregular polyhedra. These have one kind of vertex and one kind of edge but two kinds of face so transitivity 1 1 2. Searching using these criteria will find the cuboctahedron 3.4.3.4 cuo, and the icosidodecahedron, 3.5.3.5 ido. It is not hard to show that these are the only possibilities. Their duals have transitivity 2 1 1 and are the rhombic dodecahedron rdo and the rhombic triacontahedron trc. If you search for structures with two kinds of vertex, one kind of edge and one kind of face, you will retrieve three structures. The third is the adamantane cage ada; this is not a polyhedron in the strict sense as some vertices are divalent.

Archimedean polyhedra. These have one kind of vertex and more than one kind of face. By convention these do not include the infinite families of prisms and antiprisms which have one kind of vertex and two kinds of edge and face (transitivity 1 2 2). See e.g. the square antiprism **sap** and the hexagonal antiprism **hap** and the trigonal prism **trp**. **Deltahedra.** These are polyhedra with faces that are equilateral triangles. There are eight

Deltahedra. These are polyhedra with faces that are equilateral triangles. There are eight of them that are convex More below).

Frank-Kasper polyhedra. These are simplicial polyhedra with 5- and 6- valent vertices such that no 6-valent vertices are adjacent. They are [3²⁰] ico (icosahedron), [3²⁴] fkf, [3²⁶] zap and [3²⁸] mcp. You can find them as name include "Frank-Kasper" [*Hint*; in searching using "name contains" just a few symbols suffice, in this case "k-k" would do.] These polyhedra are very important in the structural chemistry of intermetallic compounds. Their duals are simple polyhedra with 5- and 6-sided faces with no two 6-sided faces adjacent. They are dod, fkf-d, zap-d and mcp-d. for more polyhedra of related kinds relevant to intermetallic crystal chemistry see Bonneau, C.; O'Keeffe, M. *Inorg. Chem.* 2015, 54, .

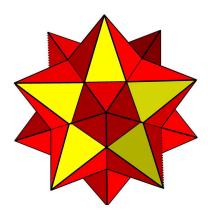
Polyhedra with faces that are squares and equilateral triangles. Those with one kind of vertex are triangular prism, **trp**, 3.4²; rhombicuboctahedron, **rco**, 3.4³; square antiprism, **sap**, 3³.4; snub cube, **snc**, 3⁴.4; cuboctahedron, **cuo**. 3.4.3.4. Missing are 3².4 and 3².4². It is easy to see that these are topologically impossible (draw a triangle and the other edges incident on those three vertices and label each angle "3" or "4" according to the vertex symbol. You will see it is impossible.) There is a second uninodal polyhedron (Miller's polyhedron) 3.4³. This the only example of more than one tiling with the same single vertex symbol for tilings of the sphere plane.



Two polyhedra 3.43.On the left the Archimedean solid symmetry \mathcal{O}_h . On the right symmetry \mathcal{D}_{4d} .

DeltahedraThese are polyhedra all of whose faces are equilateral triangles. The convex deltahedra are of particular interest in chemistry as, for example, the frameworks of *closo*-carboranes. These have 4,5,6,7,8,,10,or 12 vertices. There are others that have non-convex embeddings with triangular faces. A celebrated example is Kepler's *stella octabgula* (**stk**) obtained by capping each face of an octahedron with a tetrahedron. Similarly capping the faces of a tetrahedron gives the *stella quadrangula* (**stq**) which is an important configuration in intermetallic structures. Other stellae (stars) are derived from the other regular polyhedra. They are all Catalan polyhedra (one kind of face). The stellae should not be confused with the Kepler-Poinsot stellated polyhedra. The latter have intersecting edges (forbidden in RCSR!) and faces that are star polygons (see below). **gej** is described as one of the "most spherical" polyhedra on Alan Schoen's web site.

Starting with the vertices of a regular icosahedron and join next0nearest neighbors Those (intersecting) edges form 12 pentagrams (5-cornered star polygons) that are the faces of the *stellated dodrcahedron*. We count the triangles as faces.



Weaving. If, and only if, "weaving" is selected one will access a number of finite structures that are not strictly polyhedra. Notably these are polycatenanes which are mathematical knots but which can also be considered weaving on the surface of the sphere. These, and related, structures are embedded *piecewise linear* - with straight, non-intersecting edges. **pet** and **hwd** are embeddings of the Petersen and Heawood graphs as food for thought (the chemists of the future will make such things)). The simples regular knot, **rka**, was recently synthesized by the M. Fujita group [*Nature Comm.*. **10**, 921 (2019)].

Weaving. If, and *only* if, keyword "weaving" is selected there will be found piecewise linear embeddings of knots and other finite tangles. Under development...

1-periodic

This is a new section under development. Again "weaving" selects tangles structures - now braids and chains. under development...

2-periodic NETS

Source. some nets come from the compilation in O'Keeffe, M.; Hyde, B. G. *Phil Trans*. *Roy. Soc. Lond. A* **1980**, *295*, 553-618. identified as OKH*n*. We know all topological types of tiling with uninodal or binodal 3-connected nets. These were extracted by Olaf Delgado-Friedrichs from an earlier compilation of tilings by Daniel Huson (Geometriae Dedicata **47**: 269-296, 1993.). See also the next reference.

Uniform tilings. Uniform tilings are tilings by regular polygons. Strictly speaking if there are k > 1 vertices they should be called k-uniform. With k = 1 they are the familiar regular and Archimedean (or Kepler, who first enumerated them) tilings. All 20 for k = 2 are also there. For all k = 1-3 see Chavey, D. *Computers Math. Applic.* **1989**, 17, 147-165.

5-6-7 nets. The regular 3-coordinated net **hcb** is a tiling by hexagons (honeycomb, graphene layer). There are related 3-coordinated nets containing 5- and 7-gons as well as 6-gons. The 5-gons and 7-gons must occur in equal numbers (and it appears that there must be at least two of each in the unit cell). See **fss**, **hnc**, **hnd**, **hne**, **nnf**. They are of potential interest as the structures of low-energy 2D foams or carbon layers or as silica double layers.

4-5-6-7-8 net. The 3-coordinated net **ply** is a pretty example of tiling by almost regular polygons of different sizes. It would be nice if it came from a crystal structure but in fact I found it in D. Wells, *The Penguin Dictionary of Curious and Interesting Geometry*, Penguin 1991 page 249.

dense square nets. esq and suz are of interest as dense nets with square symmetry. The vertices are the centers of unit circles in a dense circle packing. O'Keeffe, M.; Treacy, M. M. J. Acta Cryst. 2010, A66, 5-6 for related quasicrystalline layers.

Tetragonal tungsten bronze. net **pnc** is the net of O atoms in a layer of the celebrated tetragonal tungsten bronze (TTB) structure.

Cairo tiling. The net **mcm** is an example of a tiling by congruent pentagons. It is a conspicuous feature of Cairo, Egypt sidewalks, hence the name. It is the dual of 3².4.3.4 (**tts**). It is also called MacMahon's net for the distinguished mathematician who called attention to it in *New mathematical Pastimes*.

Pentagon tilings. Another example of tiling by pentagons is **fsz-d** the dual of 3^4 .6. If we want tilings by pentagons all related by symmetry (*isohedral* tilings) then there are only one more other than $\mathbf{mcm} - \mathbf{cen-d}$ the dual of $3^3.4^2$ (\mathbf{cem}). One often sees stated that there are 14 tilings of the plane by congruent pentagons. Most of these are not *edge-to-edge* (i.e. each edge common to exactly two tiles) in contrast to all 2D tilings in RCSR, and for some of the others the tiles are congruent but not related by symmetry (and now called *monohedral*). A lovely Wikipdia site is

https://en.wikipedia.org/wiki/Pentagonal tiling

The pentagon tilings in RCSR are the duals of 5-c tilings by triangles. squares and hexagons. These are rather rare: 3, 2 and 3, with 1, 2, oe3 vertices.

Circle-packing nets (CP nets). A circle packing is a packing (on the Euclidean plane in this instance) of equal diameter circles in contact. The centers of the circles are nodes of a net and contacts correspond to links. A circle-packing net is then one that has an embedding with equal-length links that are the shortest distance between nodes. In a **stable circle packing** all tiles are strictly convex(angles between adjacent edges < 180°). It is believed that RCSR contains all uninodal and binodal stable circle packings. A **near circle packing** net (NCP) has an embedding with equal edges that are the shortest distances between vertices but there are also some unlinked vertices the same distance apart.

Self-dual tilings. These are of interest for several reasons. In chemistry a number of the most-common crystal structures can be described as a stacking of self-dual tilings with the vertices of one layer being in the position dual to the layers above and below. A dozen such were described by O'Keeffe, M. *Aust. J. Chem.* **1992**, *45*, 1489-1498. More are in O'Keeffe, M.; Hyde, B. G. *Crystal Structures I. Patterns and symmetry*. Amer. Min. Soc. 1996. The name of these tilings corresponds to the name of the crystal structure type in the cited reference. Self-dual tilings are also of interest in mathematical physics. See Kotecky, R.; Sokal, A. D.; Swart, J. M. *Commun. math. Phys.* **2014**, *330*, 1339-1394. For a self-dual tiling the average ring size must be 4 so that, except for 4⁴, there must be triangular tiles. In RCSR they have symbols beginning with **sd**. All uninodal, binodal, and trinodal are described by O. Delgado-Friedrichs & M. O'Keeffe, *Acta Crystallogr. A***73**, 14-18 (2017).

Weaving

If, and only if, this key word is selected a group of 3-dimensional 2-periodic structures are returned. They include weavings of threads, in which case the coordinates of "vertices" are actually the coordinates of points on the thread at crossing points. Also included are structures of linked polygons ("chain mail") and interwoven 2-periodic nets (sql and hcb) that have embeddings with non-intersecting straight edges. The main purposes of these are to record the symmetries which are those of the layer groups and to illustrate the patterns. Weavings are, of course, 3-dimensional. The ones listed here are 2-periodic and their symmetries are layer groups.

For an account of vertex-and edge-transitive piecewise linear embeddings see M. O'Keeffe & M. M. J. Treacy (2020) *Acta crystallogr*. A**76**, 110-120.

3D (3-periodic) NETS

Regular nets. Starting in 2003 (Delgado-Friedrichs et al. Acta Crystallogr. 2003, A59, 22-27) a systematic classification of three-periodic nets was attempted. The five regular nets have regular coordination figures¹ (regular polygon or polyhedron). They have one kind of vertex and one kind of edge and their natural tiling has one kind of face and one kind of tile (transitivity 1111). These can be retrieved using the keyword "regular". They are: 3-coordinated srs, square 4-coordinated nbo, tetrahedral 4-co-ordinated dia, octahedral 6-coordinated pcu, cubic 8-coordinated bcu. There is also one quasiregular net fcu whose vertex figure is a cuboctahedron (a quasiregular polyhedron) and the structure is 12-coordinated. This has transitivity 1112 (the 12-coordinated fcu is the net of face-centered cubic lattice whose natural tiling consists of tetrahedra and octahedra).

Semiregular nets. these have one kind of vertex and one kind of edge. transitivity $1 \ 1 \ r \ s$. Example **qtz** (quartz) **sod** (sodalite).

What every child should know about nets. Everyone should be familiar with these nine nets. They all have a unique proper tiling (one with the full symmetry of the net). The "dual" net is the net of the dual of the proper tiling. A net and its dual define a periodic surface that separates the two nets. The surfaces below are *minimal* surfaces – they have embeddings with everywhere zero mean curvature. **flu** is the only net with transitivity 2 1 1 1. **sod** is the net of the only uninodal and isohedral simple tiling. The dual, **bcu-x**, is body-centered cubic with the 8 first and 6 second neighbor links as edges (14-c). It is the only uninodal isohedral tiling by [3⁴] tetrahedra.

net	symm	CN	transitivity	dual	surface	genus
srs	<i>I</i> 4 ₁ 32	3	1111	srs	G	3
nbo	$Im \overline{3}m$	4	1111	bcu	I-WP	4
dia	$Fd\overline{3}m$	4	1111	dia	D	3
pcu	$Pm \overline{3}m$	6	1111	pcu	P	3
bcu	$Im \overline{3}m$	8	1111	nbo	I-WP	4
fcu	$Fm \overline{3}m$	12	1112	flu	F-RD	6
flu	$Fm \overline{3}m$	4,8	2 1 1 1	fcu	F-RD	6
sod	$Im \overline{3}m$	4	1 1 2 1	bcu-x	O,C-TO	7
bcu-x	$Im \overline{3}m$	14	1 2 1 1	sod	O,C-TO	7

Other tilings 1111. the net lcy has a not natural, but proper tiling of this sort (tiling ignores the 3-rings of the structure. **fcu** also has a tiling 1 1 1 1 with symmetry $Pa\ \overline{3}$. See Bonneau, C; O'Keeffe, M. *Acta Cryst*. Ab 2014, 71, 82-91. If one allows tiles that are infinite in one

¹ In the present context we can define the vertex figure as the figure defined by (better, the convex hull of) the midpoints of the edges incident on that vertex. We need to be more specific if edges are not all equal (as here).

direction (rods) then **lcs** also has tiling 1 1 1 1. Delgado Friedrichs, J. Plover and M. O'Keeffe . Acta Crystallogr. A58, 77-78 (2002).

Isohedral tilings by tetrahedra. there are exactly nine. The duals are the nine uninodal simple tilings (look for keyword "simple tiling" and no. vertices = 1). Delgado-Friedrichs, O; Huson, D. H. *Discrete Comput. Geom.* **1999**, *21*, 299-305.

hidden keywords. There are certain "names" that act as keywords, but are invisible to the user. You just have to know them. Some are:

square. This will retrieve nets with planar 4-coordination at every vertex.

icosahedron. this will retrieve nets with icosahedral groups of twelve vertices.

silica. this will retrieve nets of framework silicates etc. that are not zeolite nets (e.g. that of quartz, qtz).

iso14. This will retrieve the isohedral simple tilings by tiles with 14 faces alpha cage, FAU cage, C60, hexagonal barrel, tennis ball will retrieve structures with one of these cages. There are four structures with C_{60} (truncated icosahedra) tiles: \mathbf{csi} , \mathbf{csp} , \mathbf{fvh} , and \mathbf{fvi} .

ST-net (note the hyphen) will retrieve nets with mixed square and tetrahedral coordination

Structures with transitivity n+1 n r s. "minimal transitivity nets". For a discussion of the minimal transitivity principle in crystal chemistry see Li, M. et al. Chem. Rev. 2014, 114, 1343-1340. viv is a sphere packing net with transitivity 5 4

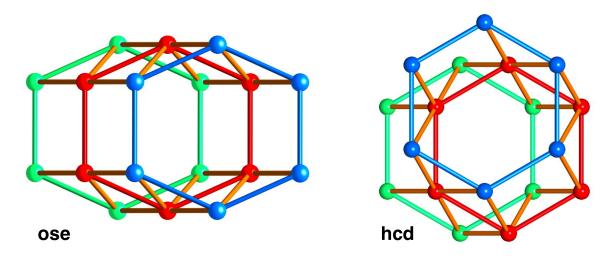
Bipartite nets. In bipartite nets the vertices can be divided into two groups say "cations" and "anions" so that all edges join a cation to an anion.

Closest packings. The closest sphere packings are familiar 12-coordinated structures. Most notably **fcu** cubic closest packing in which the sphere centers are at the points of the face-centered cubic lattice. This is the only lattice packing with maximum density but there are infinitely more with the dame density known as Barlow packings. The only one of these with one kind of sphere (nets with one kind of vertex) other than **fcu** is hexagonal closest packing **hcp**. Other closest packings can be described as composed of h layers and in **hcp** and c layers as in **fcu**. Those with two kinds of vertex are **tcj** (hc), **tck**(hcc), **tcl** (hhc), **tcm** (hhcc). See OKH Chapter 6.

The -6 family. The closest packed structures other than fcu (cubic closest packing!)) are trigonal or hexagonal and the axial ratio is $c/a = N\sqrt{(2/3)}$ where N is the number of layers normal to c in the repeat unit. If the value of c/a is reduced by a factor of 2 while keeping the other structural parameters the same, one gets a 6-coordinated family of structures. Vertices in c layers now have octahedral coordination and vertices in h layers have trigonal prismatic coordination. The structure thus derived from fcu is pcu (vertices on a primitive cubic lattice) and that from hcp is acs (the only semiregular net with trigonal prismatic coordination). Those with two kinds of vertex are hc-6 nia (the idealized NiAs structure), hcc-6 sta, hhc-6 stb, hhcc-6 ste. Just as NaCl is the binary version of pcu, so WC is the binary version of acs. TiP has the ste (hccc-6) structure – actually ternary. MOFs (cobalt

formates) based on these structures were reported by Shang et al. APL Materials **2014**, 2, 124104.

Stacked 6³ (honeycomb) nets. 6³ nets can be packed in the same way as 3⁶ nets in close packing so that each vertex has seven nearest neighbors. The density is ideally 2/3 that of closest-packing, but for some configurations there is a slightly lower density embedding with the same symmetry and seven equal edges. For AB (h) packing there are two uninodal packings **osf** and **wkv**. For ABC (h) packing there is one uninodal net **ose** and one binodal structure **hcd**. See figure below. Other binodal structures are: **hci** (h) hcj (h) and h0 hcj (h1 hcc). For a reason why these nets might be interesting see: h1. h2 hys. **102**, 093511 (2008). In RCSR search by "name contains" = "h3".



Uniform tiling. If you click on the "keyword" in the nets search page you will find the following information for the 28 uniform tilings:

In a uniform tiling, all the vertices are the same (uninodal or vertex transitive) and the tiles are all uniform polyhedra (vertex transitive with regular polygonal faces). Grünbaum, B. *Geombinatorics* **1994**, *4*, 49-56. Deza, M.; Shtogrin, M. *Eur. J. Combinatorics* **2000**, *21*, 807-814.

The correspondence with Grünbaum's numbers are: 1: fcu 2: hcp 3: tcd 4: tca 5: flu-e 6: crs 7: reo 8: cab 9: reo-e 10: ubt 11: hex 12: tsi 13: svk 14: sve 15: svh 16: tfs 17: svj 18: kag 19: ttw 20: pcu-i 21: hal 22: pcu 23: fst 24: fee 25: lta 26: hex 27: rho 28: sod

Tiling with regular polygon faces. The uniform tilings are vertex-transitive ND all faces are regular polygons. additional tilings of this sort are those of **nia-e** and **wng**. These contain isomeric Johnson polyhedra (polyhedra with regular faces) with 18 faces; not in themselves vertex transitive, but the tilings are. It might be nice to know all such tilings (*hint*).

A remarkable tiling that "almost" has faces that are regular polygons is that of the binodal net **bon** in which the tiles are rhombicuboctahedra, cuboctahedra, octahedra and square antiprisms. It is easy to see that the faces aren't exactly regular. (a) square antiprisms have non-crystallographic symmetry and (b) the structure has four edges but only three degrees of freedom. A more subtle case is $\mathbf{fub} = \mathbf{sod}$ - \mathbf{e} - \mathbf{a} . This is a tiling by trigonal prisms,

truncated tetrahedra and a large polyhedron (**tro-e-a**) with 4-, 6-, 8-, and 12-sided faces. The coordinates are fixed by the requirement of equal edges, but it will be found that the polygons, other than the square, are not quite regular or even planar,

mog-e-x-z. This is the idealized net (regular tetrahedra) of the anions in the moganite form of silica (also in BeH₂). Why the bizarre symbol? mog is the topology of the 4-coordinated net of the Si atoms. In the maximum symmetry (*Cmmm*) embedding of the net mog-e (q.v.) some of the tetrahedra collapse to squares. To get the topology of the tetrahedra we need to add the diagonals of the squares as edges and the net symbol would be mog-e-x (extended structure) but now we have edges intersecting and tetrahedra of zero volume so we go to a lower symmetry (*Ibam*) embedding which allows regular tetrahedra and add -z to the net symbol. Incidentally *Ibam* is the symmetry of crystalline BeH₂. Moganite is even lower symmetry (monoclinic) to allow the Si-O-Si angles to come to preferred values (about 145°). See *Phil/Trans.* 2014, 372, 20120034.

Uninodal 3-coordinated tilings of D, P and G surfaces. Possibly the only uninodal structures of this type are the polybenzene family 6.8^2 pbz, pbp and pbg which have the full symmetry of the surfaces $(Pn \ \overline{3}m, Im \ \overline{3}m, Ia \ \overline{3}d)$ and the 9^3 family uta, utb and utc which however have lower symmetries $(Fd \ \overline{3}m, I432 \ \text{and} \ I4_132)$. For a 7^3 tiling (not uninodal) of P see kgn. For more such search for e.g. name contains 9^5 .

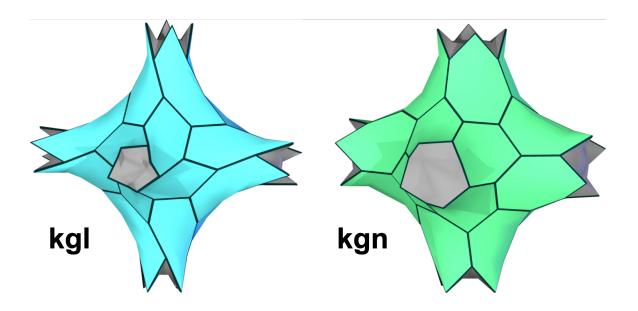
4-coordinated tilings of D**,** P **and** G **surfaces.** There are many of these. A good example is the trio **ukd**, **rho** and **gie** which are $4^3.6$ tilings of P, D and G respectively . There are two distinct uninodal $4^3.6$ tilings of the hyperbolic plane, the second gives **fau** as a tiling of D. (what are P and G structures?), See J. Solid State Chem. **2005**, 178, 2533-2554. The net, **tsc**, of the zeolitic mineral tschortnerite, is a tiling of the F-RD surface.

5-coordinated tilings of P **and** I**-WP surfaces.** There are infinitely many 3.4 4 tilings of the P surface with regular polygons. **pcu-i** is the only uninodal one, See **mjy** and **mjz** for other examples. **fcp** is 5 5 self-dual tiling of I-WP (vertex and face transitive as 2D tiling)

Two 3^2 .4.3.6 tilings of G. These are the nets fcy and fcz, Although there is only one hyperbolic tiling 3^2 .4.3.6 there are two distinct projections on the G surface. This property arises for an chiral hyperbolic tiling; see Eur. Phys. J. 2004, B39, 365. fcz is the underlying topology of a porous germanate with a giant cubic cell (see references).

Tilings of *CLP***.** This tetragonal minimal surface of genus 3 has **cds** as its labyrinth graph. **abr** is a tiling of the surface by quadrilaterals and hexagons with 4.6.4.6, $4^2.6^2$, and 4^4 vertices.

 7^3 tilings of P. Tilinggs 3^3 , 4^3 , 5^3 (of the sphere) and 3^6 , 4^4 and 6^3 (of the plane) are unique. But there are multiple ordered (vertex-transitive) tilings 3^6 , 4^4 and 6^3 of the cylinder (see 1-periodic). But tilings of periodic surfaces are more complicated. For example there (at least!) two cubic [7^{24} .86] tiles that fit together to make 7^3 tilings of P. But the two units can be combined (see **kgs**) in any proportion to make tings that may well be disordered (only trivial symmetry). See below



Subnets of bcu. Nets of embed type 2 can be derived from **bcu** by systematically deleting links to produce *subnets* (or *subgraphs*). Examples are **bcs**, **rob**, **sxa**, **loh**, **lom**. **dia-c** has two disjoint subnets, linking them with one extra link gives the 5-coordinated structures **fnu** and **fnx**. See V. A. Blatov. *Acta Cryst. A***63**, 239 (2007).

Subnets of fcu. Nets of embed type 2 can be derived from **fcu** by systematically deleting links to produce subnets. Examples are **hxg**, **lsz**. **srs-c4** has four disjoint subnets as does **srs-c4***.

Subnets of pcu. Nets of embed type 2 can be derived from **pcu** by systematically deleting links to produce subnets. Examples are **cds**, **cdl**, **cds-f**, **fsc**, **fsg**, **pto-d**.

Vertices with the same vertex symbol and coordination sequence. See ana-f, ana-a edq cdj, ffi tff, ffg ffj. bwt is a binodal net with the same vertex symbol and coordination sequence for each node.

Monoclinic with $\beta = 90^{\circ}$. Some monoclinic crystals have β very close to 90° (β -Ga₂O₃ is a good example). The net **vna** has β also very close to (exactly equal to?) 90° in its minimum density embedding.

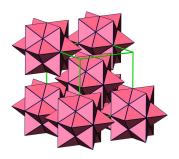
Rod packing and Diamond/quartz relation. There are four distinct 2-way (rods running in two different directions) packings of equivalent rods. There are two pairs in which there is a tetragonal and a hexagonal packing. nets based on these packings come in pairs The following pairs have symmetry $I4_1/amd$, $P6_222$: ant, anh; ths, bto The following pairs have symmetry $P4_2/mmc$, $P6_222$: cds, qzd; pts, pth

1/2 transitive graphs. A vertex-transitive graph is said to be 1/2 transitive if it is also edge-transitive, but not arc transitive (an arc is an edge with a direction). The nets of RCSR are

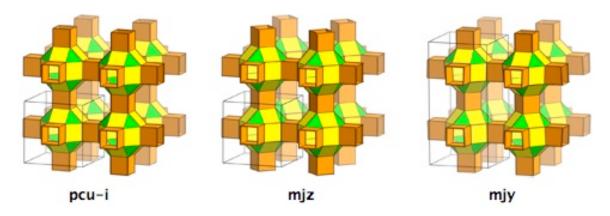
graphs and there are just two that are 1/2 transitive, or, in other words, that have polar edges. They are **ana** and **thp**.

Edge but not vertex transitive graphs. In graph theory the are sometimes called semisymmetric graphs. Nets that are edge transitive but not vertex-transitive must have two kinds of vertex. Ignoring nets with symbols having extension -b there are just four nets of this type in RCSR with the same coordination number for each vertex. They are pth, pts, ssb and ssc - all 4-coordinated.

A [3⁴⁸] tiling (xam) with transitivity 2211. What is the dual? The answer is bcu (bodycentered cubic lattice with 6-fold edges. Pairs of tiles have six faces in common.

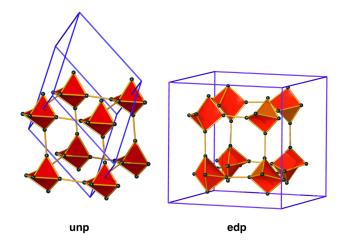


3.4⁴ tilings of P. The structure **pcu-i** is the net of a uniform tiling (q.v.) – the tiles are cubes, truncated cubes, octagonal prisms and rhombicuboctahedra. It can also be thought of as a uninodal 3.4⁴ tiling of the P surface using equilateral triangles and squares. There are infinitely many variants of this 3.4⁴ tiling using regular triangles and squares. To simple examples are shown by **mjz** (see reference) and **mjy**.



Linking trigonal prisms with pcu topology

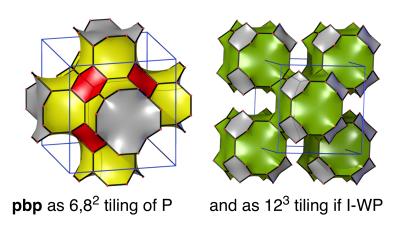
There are more than one way of doing this. In Chem. Rev. 112. 675 (2012) figure 24 the binodal **edp** (symmetry Pa-3) is misidentified as the uninodal **unp** (symmetry R32)



Nets with collisions

nets with collisions are those in which two or more vertices have the same coordinates in barycentric coordinates. In *non-crystallographic nets* there are isometrics of the net x that are not crystallographic symmetries - **bad** is an example. **uld-z** is a *ladder*, which has two or more copies of subnets separated by a vector \mathbf{r} and extra link ("rungs") along \mathbf{r} linking the subnets. **rld-z** is interesting because it has subnets linked by edges that are not along \mathbf{r} . The subnets still collapse onto each other in barycentric coordinates but the symmetry is crystallographic ($Im \ \overline{3}m$ in **rld**). However in this maximum symmetry there are edges of zero length. See *Acta Cryst*. **2013**, *A69*, 535-542 for examples of nets of this kind that appear in real materials.

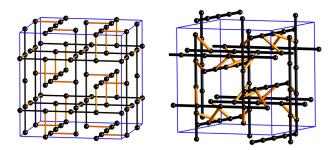
An infinite polyhedron 3^{12} . xii is the net of a vertex- and face-transitive infinite polyhedron that is a tiling of the *I-WP* surface. The dual is a 12^3 tiling of the same surface. The net of this is **pbp** which is of course a 6.8^2 tiling of the *P* surface! but **pbp** (vertex symbol 6.8.8) also has a 12-ring at each angle and the same net serves for two polyhedra: 12^3 tiling of *I-WP* and 6.8^2 tiling of *P*. It is instructive to use 3dt to draw both these tilings using the data for the tiling of **pbp** as shown here:



Triclinic nets. There are only two triclinic nets in RCSR. **nch** is the unique triclinic uninodal sphere packing (Werner Fischer). **rug** is a remarkable simple tiling by one topological kind of 14-face simple polyhedron with four topologically-distinct polyhedra in the packing (monohedral but not isohedral tiling). Discovered by Ruggero Gabbrielli. See references provided in RCSR. **rug** is one of the most complex nets in RCSR. Transitivity 24 48 32 4. (Slightly more complex are **tei** and **tep** of interest as theoretical Frank-Kasper phases). See also occurrence of space groups (below).

Uninodal polar nets. It is interesting that it is possible to have uninodal polar 3-periodic structures. Note that to have a polar *finite* structure (molecule) there must be at least two kinds of vertex (atom). But for infinite periodic point sets, uninodal polar structures are possible in 14 of the 58 polar space groups (this includes four enantiomorphic pairs). These are *Fdd2*, *P4*₁, *P4*₃, *I4*₁*md*, *I4*₁*cd*, *P3*₁, *P3*₂, *R3*, *R3m*, *R3c*, *P6*₁, *P6*₅, *P6*₂, *P6*₄. Indeed the RCSR lists 21 polar uninodal nets. But note that when we consider uninodal *connected* point sets (nets) all symmetries other that *P1* are possible

Minimal density. The embedding of a net in RCSR is that for equal edge if possible and for those which still have degrees of freedom the density is minimized. The binodal 3-c net **bwt** is unusual in not having a single configuration of minimum density. 2/3 of he links of the net fall on rods along ,100>. At minimum density the rods are straight, and for links of nit edge the unit cell edge is 4.0. For this (symmetry $Pa\overline{3}$) the vertices are at x, y, 1/4 and x+1/4, y, $\frac{1}{4}$. for straight rod (minimum density) $y = (1+2x \pm \sqrt{(1+2x)^2 - 1-16x^2)})/4$. the picture n the left below is for x = y = 1/4. in the middle of the sphere packing range. on the right another minimal density arrangement.



Note that this is not a sphere-packing net – the vertices of the embedding on the left above are in the positions of the 4-c net **nbo**. So the net is derived from NbO by systematically deleting $\frac{1}{4}$ of the edges. Another net derived in the same way from **nbo** is the lovely uninodal **vab** (q.v.). Many nets in RCSR have been derived in this way by V. A. Blatov. *Acta Cryst.* **2007**, A63, 29-343; **2009**, A65, 202-212.

Net of girth 16. The girth of a net is the size of its shortest ring. The largest girth of any net in RCSR is in **sxt** which has girth 16. Another Blatov net (see above). The largest rings in a uninodal net are the 26-rings in **sin**.

Largest ring in a uninodal net. This question only makes sense if we ask for strong rings (which are not the sum of smaller rings). Even then on can make arbitrarily large rings by, for example, replacing vertices of a net by groups of vertices. See nets whose

symbol begins with "**sod-a**". Each "-a" doubles the largest ring size. But for a uninodal net the record appears to be held by **sin** which contains 26-rings (370 meet at each vertex!)..

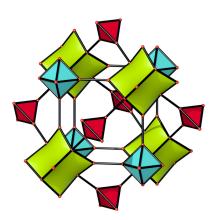
-t nets. The extension –t refers to a net derived from a tiling of a net. In the Dress approach to tiling, each tile is divided into *chambers* formed by (in 3-D) a vertex, the center of an incident edge, the center of an incident face and the center of the tile. The number of distinct chambers is the tiling size (given under "D-symbol" at the bottom of an RCSR page). The dual of the ting by those chambers gives the –t net. That net has its vertices on the surface associated with the net (see e.g. **srs-t**). See de Canpo, L. *et al. Acta Cryst.* **2013**, *A65*, 483-489. The number of vertices in the –t net is the same as the number of chambers (size) of the original; for qtz-t this is 14. Try searching for symbol contans "-t"; the nets are pretty – ans some surprises.

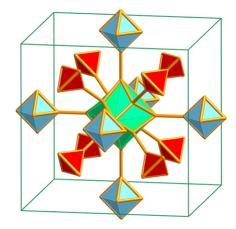
-I nets. The extension -I is another specialized one referring explicitly to 3-c tilings of 2-D surfaces. For a given 3-c tiling center every tile and form triangles from that vertex and each edge of the tile. Now one has a tiling by triangles. The dual of that is a new 3-c tiling with three times as many vertices as the original. The procedure was introduced as "leapfrog" by Patrick Fowler for fullerenes. In RCSR it is applied to some "Schwartzites" (hypothetical 3-c carbons formed by tiling periodic surfaces)

Tilings with 5-sided faces. sadly pentagonal dodecahedra do not tile Euclidean space in a tiling in which at least three faces meet at each edge. For a tiling with "two-face" edges see **cdh**. For a lovely tiling of pentagonal dodecahedra with a larger polyhedron with all 5-sided faces see **fiv**. A tiling by pentagonal dodecahedra and pentagonal tetrahedra(not polyhedra is the equally beautiful **ith-d**. [It seems likely that there is no uniform 4-c net of girth 5 - i.e. all shortest rings at each angle 5-rings]. There is a uninodal uniform 5-c net **gan** with isohedral tiling [5^4]

Tilings with 7-sided faces. itv (the net of ice-XII) has an isohedral tiling by [7⁸] tiles.

A nets with high-symmetry 10 and 14 coordination. The net xbp is a minimal transitivity (3 vertices, two edges) (4,6,10)-c net. The 10-c vertex has $\overline{4}3m$ (tetrahedral) symmetry and the coordination figure is an adamantane cage with 6 vertices arranged as a regular octahedron and 4 as a regular tetrahedron. The "octahedral" vertices are linked to octahedral vertices and the "tetrahedral" vertices are linked to tetrahedral vertices. See xbp-a shown below lest. The net wzz is (4,6,14)-c again with minimum transitivity (3 2) and the 14-c coordination figure is a rhombic dodecahedron—see wzz-a below right.





Homometric structures. In the early days of x-ray diffraction (before direct methods) there was discussion of whether two different crystal structures could have the same diffraction pattern (and thus the same Patterson map). Such structures, called homometric, are rare but do exist. The simplest homometric pair of closest (Barlow) packings have 15 layer sequences [Mardix, S. *Acta Cryst.* 1990, *A46*, 133-138. A good place to learn about descriptions of close packings.]. Two simple structures in RCSR are homometric lcs and lcv-c. The nodes of these in the most symmetric embedding are the invariant lattice complexes *S* and *V**. They are obviously different patterns (one contains 3-rings, the other doesn't) but they are homometric (have the same sets of inter-node vectors). *Homeomtric* has a different meaning.

Simple tilings and foams

A *simple* polyhedron has two faces meeting at an edge and three faces meeting at a vertex (3-c). In a *simple tiling* of 3-D Euclidean space, two tiles meet at a face, three at an edge and four at a vertex. It is the dual of tiling by tetrahedra. A *foam* has the topology of a simple tiling but the dihedral angles at the edges are $\cos^{-1}(-1/2) = 120^{\circ}$ and the angles at the vertices are $\cos^{-1}(-1/3) = 109.5^{\circ}$. Accordingly, the faces and edges are curved and the faces have constant mean curvature.

We know of two duals of tilings by tetrahedra (**bcr** and **bda**) in which the tiles are not polyhedra in the strict sense as their 1-skeleta (graphs) are not 3-connected. See Delgado-Friedrichs, O.; O'Keeffe, M. *Acta Cryst.* **2005**, *A65*, 58-62. In general simple tilings will not be realizable with convex polyhedra anyway (see below).

Space-filling solids: Isohedral and monohedral tilings and parallelohedra. A

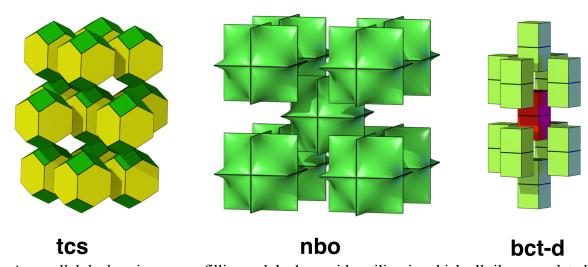
A good reference is *Tiling with congruent tiles*, Grünbaum, B.; Shephard G. C. *Bull. Am. math. Soc.* **1980**, *3*, 951-973.

A monohedral tiling is one in which all tiles are topologically the same. For example tilings by tetrahedra [3⁴].

An *isohedral* tiling is one in which all tiles are related by symmetry ("kinds of tile" = 1 in RCSR). RCSR lists all isohedral simple tilings by tiles with 14 faces (the smallest possible number of faces) See Delgado-Friedrichs, O.; O'Keeffe, M. *Acta Cryst.* **2005**, *A65*, 58-62. There is only one uninodal isohedral simple tiling (**sod**). There are 11 binodal isohedral simple tilings all in RCSR (keyword "simple tiling", "kinds of vertex" = 2, "kinds of tile" = 1).

A convex isohedral tile is known as a *stereohedron*.

A remarkable monohedral simple tiling by 14-face tiles with tile transitivity 4 was discovered by Ruggero Gabrielli. See **rug** in RCSR. This polyhedron has no isohedral tiling.



A parallelohedron is a space-filling polyhedron with a tiling in which all tiles are related by translations. It has long been known (Federov, 1885) that there are only five topologically-distinct such tilings by convex polyhedra. By cubes $[3^8]$ **pcu**, by hexagonal prisms $[3^6.6^2]$ **bnn**, by rhombic dodecahedra $[4^{12}[$ **flu**, by truncated octahedra $[4^6.6^8]$ **sod**, and by elongated dodecahedra ("hexarhombic dodecahedra" = $[4^8.6^4]$). Net = **tcs**. The centers of the tiles form a lattice (in the strict sense of one point per primitive cell). These are respectively: primitive cubic, hexagonal, face-centered cubic, body-centered cubic (considered as 14-coordinated) and tetragon ally-distorted face-centered cubic. The **nbo** tile $[6^8]$ is a generalized paralellohedron (not strictly a polyhedron as it has 2-c vertices) with centers forming the 8-c **bcu** structure. The 10-c body-centered tetragonal lattice net **bct** is generated as the dual of a $[4^{10}]$ "double cube" tiling as shown above. Having contiguous faces co-planar excludes convexity. Of course, **bct-d** has the same net at **pcu**.

An interesting paper Fortes, M. A.; Ferro, a. c. Z. Kristallogr. 1985, 173, 41-57 showed how to generate simple (3-c) parallelohedra of arbitrarily number of faces. Crystallographic data for some of these were given by O'Keeffe, M. Kristallogr. 1999, 214, 438-442. Two in RCSR are kto (20 faces) and kts (26 faces). Clearly these tilings can't be realized with convex tiles.

Occurrence of space groups. some symmetries are more suitable than others or crystal structures. There is a large literature on the subject. Organic crystals (of the order of 10^6 known) are composed of molecules with generally only trivial symmetry (1) and the most common symmetries are first $P2_1/c$ and next $P\overline{1}$. Brock, C. P.; Dunitz, J. D. *Chem. mater.* **1994**, 5, 1118. For inorganic crystals the most common symmetry is *Pnma* followed by $P2_1/c$ again. Baur, W. H.; Kassner, D. *Acta Cryst.* **1992**, *B48*, 356. We have noted that the intermetallic structures have high symmetry generally tetragonal, hexagonal or cubic in classes 4/mmm, 6/mmm and $m\overline{3}m$ (holohedral symmetry). Bonneau, C.; O'Keeffe, M. *Inorg. Chem.* **2015**, .What about RCSR? The results are skewed by the propensity of certain

space groups to have many uninodal sphere packings but generally the "interesting" nets (the aim of RCSR is to collect these) have high symmetry. In RCSR the most-common symmetries are $I \ m \ \overline{3}m$ and $P6_3/mmc$ (about 6% each). These are followed closely by $I4_1/amd$ and I4/mmm. Next is $P6_222$, by far the most common chiral symmetry in RCSR. By contrast for organic and inorganic crystals it is $P2_12_12_1$ which has no entries in RCSR. About one half of the space groups have 0 or 1 entry in RCSR.

Quotient graph, genus, and complete graphs

The quotient graph of a net is a finite graph in which a vertex replaces all translationally-equivalent vertices of the net. The edges are labeled to denote he translation between connected vertices. Thus vertex 1 might be connected to vertex 2 in the unit cell displace by a translation 100, and the edge is labeled accordingly. [Chung et al. Acta Cryst. A40, 42 (1984). The number of numberings and labeling for the quotient graph of a given net is infinite but there is a canonical form ("Systre key") used by Systre to identify nets. (Export from Systre as "abstract topology").

A complete graph K_n , is a finite graph with n vertices in which every vertex is connected to every other. For a given number of vertices it is the most "symmetrical". "Symmetry" in this context, better "automorphism", means permutations of the vertices that leave the adjacencies (edge) unchanged. In thee case of K_n , he automorphism form a group of order n!. The cyclomatic number. g, of K_n is the number of independent cycles: g = 1 + e - v = (n-1)(n-2/2)

In RCSR the chromatic number of the quotient graph is called the genus. For a 3-periodic graph the minimal genus is 3 and each net of genus 3 ("minimal net") has a unique quotient graph. Famously, **srs** is the unique graph with K_4 as quotient graph. For more on Minimal nets see de Campo et al. Acta Cryst. A69, 483 (2013) and references therein.

Not very useful information: In RCSR there are five graphs with K_5 and five with K_6 as quotient graph. None with K_7 and two with K_8 . [look for name – "K5 net" etc].

The invariant straight line structures

There are two kinds of periodic structure composed of straight lines: those in which the lines intersect and those in which they do not. In invariant structures the positions of the lines are fixed by symmetry. In non-intersecting line structures the lines correspond to the axes of cylinders in a cylinder packing.

The 12 invariant packings are described in *J. Am. Chem. Soc.* **2005**, *127*, 1504. Four correspond to parallel rods intersecting a plane in the positions of the invariant lattice complexes of 2 dimensions. These are **sql** (square lattice), **hxl** (hexagonal lattice).**hcb** (honeycomb) and **kgm** (kagome)..

To find many-way structures in RCSR look for keyword "rod net"

There are four 2-way structures illustrated as nets with links corresponding to points of contact. Two are tetragonal: **ths-z** and **cds** and two are hexagonal **bto-z** abd **qtz** in very case the rods corresponding to the axes of cylinders in contact are normal to **c**.

There are two cubic 3-way structures with lines along <100>: **bmn** and **nbo-z**. These were earlier (*Acta Cryst.* **2001**, *A57*, 110) given symbols Π and Π *.

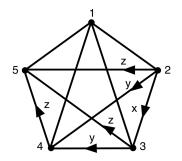
There are four 4-way structures with lines along <111>.: gan (Γ) , utb-z (Ω) , sgn-z (Σ) and sgn-z-c (Σ^*) ; the last corresponds two interpenetrating cylinder packings.

Earlier descriptions of invariant line structures with intersecting lines have not been found. These are of the sort pq which indicates that the lines run in p directions and q meet at each intersection. 13 are listed here. Strictly **rhr** does not belong as the extra condition of straight lines is required to fix the coordinates

type	pq	net	symmetry	coordinates
square 2-way ,<10>	22	sql	p4mm	0,0
hexagonal 3-way ,<10>	32	kgm	р6тт	1/2,0
	33	hxl	р6тт	0,0
tetragonal 4-way, <101>	42	lvt	I4 ₁ /amd	0,0,0
cubic 3-way, <100>	32	nbo	$Im \overline{3}m$	1/2,0,0
	33	pcu	$Pm \overline{3}m$	0,0,0
cubic 4-way, <111>	43	bcs	Ia ₹3d	0,0,0
	44	bcu	$Im \overline{3}m$	0,0,0
cubic 6-way, <110>	62	rhr	$Im \overline{3}m$	1/3, 1/3,0
	63	hxg	$Pn \overline{3}m$	0,0,0
	63	crs	$Fd\overline{3}m$	0,0,0
66	64	reo	<i>Pm</i> $\overline{3}$ <i>m</i>	1/2,0,0
	66	fcu	<i>Fm</i> $\overline{3}$ <i>m</i>	0,0,0

K5 carbon

This is really a joke. The net **edi** has as quotient graph the complete graph on 5 vertices K_5 . Here it is shown with the labeling according to the Systre key, "x", "y" and "z" refer to 100, 010 and 001 and unlabeled edges are 000.



Inorganic crystal structures with (fairly) simple nets

formula	name	net	coordination	transitivity
NaC1	halite	pcu-b	6-6	2 1
WC	-	acs-b	6 -6	2-1
CsCl CuZn	β-brass	bcu-b	8-8	2 1
ZnS	sphaleride	dia-b	4-4	2 1
ZnS	wurtzite	lon-b	4-4	2 2
PtS	cooperite	pts	4-4	2 1
BeO	β-BeO	crb-b	4-4	2 2
FeSi		svn-b	7-7	2 2
PdF ₂	-	pyr	3-6	2 1
CaF ₂	fluorite	flu	4-8	2 1
TiO ₂	rutile	rtl	3-6	2 2
TiO ₂	anatase	ant	3-6	2 2
PbO_2	α -PbO ₂	apo	3-6	2 2
Al_2O_3	corundum	cor	4-6	2 2
Ni ₄ S ₃	heazlewoodite	hea	4 -6	2 2
FeS_2	pyrite	fsn	3-6	2 2
FeS_2	marcasite	mrc	3-6	2 3
Th ₃ P ₄		tph	6-8	2 2
Cu ₃ Au		ftw	4-12	2 1
CuFeS ₂	chalcopyrite	dia-b3	4-4-4	3 2
NaFeO ₂	-	pcu-b3	6-6-6	3 2
AlMnCu ₂	Heussler alloy	bcu-b3	8-8-8	3 2
SrTiO ₃	perovskite	xbo	6-6-12	3 2
CaCO ₃	calcite	zxc	3-3-6	3 2
TlSe	$Tl(I)Tl(III)Se_2$	ctt	4-6-8	3 2
$KFeO_2$	-	kfo	4-8-12	3 2
K ₂ PtCl ₆		kpc	5-6-12	3 2
MgAl ₂ O ₄	spinel	spl	4-4-6	3 2
ZrSiO ₄	zircon	zrc	3-4-8	3 3
UH ₃	β-UH ₃	buh	4-12	3 3
Si ₃ N ₄	β-Si ₃ N ₄	sln	3-4	3 3
Cu ₂ ZnSnS ₄	kesterite	dia-b4	4-4-4	4 3

Intermetallic structures as foams

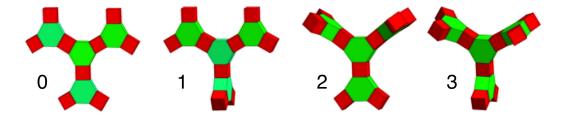
Many important intermetallic structure types are based on packings of tetrahedra. Elements (e.g. Fe) with the 14-c body-centered cubic structure (**bcu-x**) are the simplest. The "Frank-Kasper" structures are based on packings of tetrahedra in which either five or six meet at an edge. Notable are the MgCu₂ structure (the most populous binary structure type) and the Cr₃Si structure type. The dual structures are foams (simple tilings). As explained by C. Bonneau and M. O'Keeffe [*Inorg. Chem.* **54**, 808-814, (2015)] these dual structures are a

valuable aid to visualizing and understanding the structures. Simple binary examples are listed in the Table below - see the pics in the dual structures.

structure	RCSR	transitivity	dual	
Fe	bcu-x	1 2 1 1	sod	
MgCu ₂	mgc-x	2 3 4 3	mtn	
Cr ₃ Si	mep	2 3 4 3	mep	
CuAl ₂	cal	2674	cal-d	
AlB_2	alb-x	2 4 4 3	alb-x-d	
ThSi ₂	tsi	2674	sgt	
CrB		2896	cbd	

Nets formed from cubes and hexagonal prisms.

he picture sows possible ways of connecting hexagonal prims to three others with intervening cubes. The numbers are the numbers of prisms twisted relative to the central one. It should be clear that the "0" shapes can be assembled into a layer, The "1" shapes combine to form **thz**, or omitting the cubes, **thh**. It should be clear that these in turn are based on the 3-c net **ths**. The "0" and "1" shapes combine to form the net **clj**, or omitting the cubes, **cli**. It should be clear that these in turn are based on the 3-c net **clh**. The only known possibility for combining the "2" and "3" shapes is the spectacular **ucz**, or, omitting the cubes **uca**. These in turn are based on the 3-c net **xaa**. Omitting just some of the cubes produce **ucb** and **ucy**. **ucb** is the net of the remarkable ZIF-412 from the Yaghi group [JACS, **139**, 6448, (2017)]. The nets **ucw** and **ucx** cannot be made with strictly regular cubes and hexagonal prisms.



Deltahedra

These are polyhedra with equilateral triangular faces. See the entry earlier for finite deltahedra. The 1-periodic case (tilings of cylinder) is very rich in vertex and edge-transitive structures - two infinite families: The periodic achiral family and the chiral aperiodic family. The latter includes the famous Boerdijk-Coxeter helix, unfortunately out of the domain of RCSR - for their occurrence in rod-MOF structures see *Chem. Rev.* **2016**, *116*, 12466-12535.. The 2-periodic case has just one tiling 3⁶ (hxl).

For 3-periodic examples RCSR includes 12 (search for name = deltahedron). **Pda**, **pbb**, **pdm** and **dda**, **ddb** are clearly the simplest members of infinite families. Seven are vertex

transitive and three (**uty**, **utz** - 3^9 tilings of D and G, and **xii**, a 3^{12} tiling of I-WP) are also face-transitive. None are edge-transitive. **utx**, a 3^9 tiling of P, is vertex-and face-transitive but has no embedding as a deltahedron. No effort at completion has been made, so these should just be regarded as examples.

For a broader definition of deltahedra and more examples see Pedersen, M. C.; Hyde, S. T. *Proc. Nat. Acad. Sci.***2018**, *115*, 6905-6910. In that connection a lot of, er... stuff, has been written about packings of regular tetrahedra. Possibly the least dense (the interesting case) of one kind of tetrahedron is **sod-e**. Possibly the only example of vertex-, edge-, and face-transitive tetrahedron packing is **crs**. The analogous "regular" packing of octahedra is **reo**.

Weaving of threads

The line sets (above) are important in the description of weaving. In *fabric* weaving, if the threads are pulled straight they form patterns of intersecting straight lines. In *chain-link* weaving (or *knitting*), if the threads are pulled straight they pass through each other and form a pattern of non-intersecting straight lines. Liu, Y.; O'Keeffe, M.; Treacy, M. M. J.; Yaghi, O. M. (2018) *Chem Soc, Rev.* **47**, 4642-4664.

To access 2-periodic and 3-periodic weavings in RCSR select keyword "weaving". Weavings only appear when that is done. Note that polycatenanes and interpenetrating nets (symbol contains -c) are considered weavings.